

Grade 10 C
Mathematics lesson 2

Topic: Complement of a set

The complement of a set is the set of all elements in the universal set that are not members of the given set. It is denoted by ' or c.

EXAMPLE 1

1. If $E = \{a, b, c, d, e, f, g\}$, $A = \{a, b\}$ and $B = \{a, b, c, d, e\}$. find
 (a) $A' \cup B$
 (b) $(A \cup B)'$

Solution

Notes: first find the union set of B. Thereafter A' (it means elements that are not in set A. Finally form set $A' \cup B$ by combining the elements of A' and UB .

(a) $A' \cup B$ $UB = \{a, b, c, d, e\}$ $A' = \{c, d, e, f, g\}$
 $= A' \cup B = \{a, b, c, d, e, f, g\}$.

(b) $(A \cup B)' = A \cap B' = \{a, b, c, d, e\}$
 $= (A \cup B)' = \{f, g\}$. • first find $A \cup B$ then the complement.

EXAMPLE 2

2. Given that set $E = \{1, 2, 3, 4, 5, 6, 7\}$, $A = \{1, 2, 3, 4\}$, $B = \{1, 3, 4, 5\}$ and $C = \{2, 3, 4, 5\}$ list:
 (a) $(A' \cup B) \cap C$
 (b) $(B \cup C)' \cap A$
 (c) $B' \cap (A \cap C)$

Solutions

(a) $(A' \cup B) \cap C$. Notes: first deal with the set in the brackets (ie $A' \cup B$)
 $A' = \{5, 6, 7\} \cup B = \{1, 3, 4, 5\}$
 $= (A' \cup B) = \{1, 3, 4, 5, 6, 7\} \cap C = \{2, 3, 4, 5\}$
 $= (A' \cup B) \cap C = \{3, 4, 5\}$. Here check the common elements.

(b) $(B \cup C)' \cup A$. Hint: always start with the set in the brackets.

$(B \cup C)' = \{6, 7\}$ $U = \{1, 2, 3, 4\}$ $(B \cup C)'$ it means elements that are not in Set B and C.

$$= (B \cup C)' \cup C = \{1, 2, 3, 4, 6, 7\}$$

$$(C) B' \cup (A \cap C)$$

$$= A \cap C = \{2, 3, 4\} B' = \{2, 6, 7\}$$

$U(A \cap C) = \{1, 2, 3, 4, 5\}$. Find $A \cap C$. Then $U(A \cap C)$ is the correction of $A \cap C$ and the union of both sets.

$$B' \cup (A \cap C) = \{1, 2, 3, 4, 5\}$$

EXERCISE

1 Given that $E = \{1, 2, 3, 4, 5, 6\}$, $A = \{2, 3, 4\}$ and $B = \{5, 6\}$. List the sets

(a) $(A \cap B)'$

(b) $A' \cup B$

2. Given that $E = \{a, b, c, d, e, f, g\}$, $P = \{a, c, d, e\}$, $Q = \{b, d, e, f\}$ and $R = \{a, b, d, e\}$. List

(c) $(Q \cap R) \cup P'$

(b) $P' \cup (Q \cap R)$

(c) $(R' \cap Q) \cup P$

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